# S.S JAIN SUBODH P.G. (AUTONOMOUS) COLLEGE JAIPUR

# M.SC. (STATISTICS) I SEMESTER

## **ASSIGNMENT**

**Subject:- MSST-101: Statistical Mathematics** 

## UNIT: I

## Question: 1

Find the rank of given matrix

$$\begin{bmatrix}
 1 & 3 & 2 \\
 4 & 1 & -2 \\
 2 & -3 & 1
 \end{bmatrix}$$

#### Question: 2

Check the consistency of following system of linear equations and solve if the system is consistent

$$\begin{cases} 4x + 3y - 6z = 10 \\ -x + 2y - 5z = 6 \\ 7x - y + z = 8 \end{cases}$$

#### **UNIT: II**

### Question: 3

Verify Caleys Hamilton theorem for the following matrix

$$\left[\begin{array}{cccc} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{array}\right]$$

## Question: 4

Find the corresponding matrix which transforms the following matrix to a diagonal form.

$$\begin{bmatrix} -1 & 2 & -2 \\ 1 & 2 & 1 \\ -1 & -1 & 0 \end{bmatrix}$$

## UNIT: III

## Question: 5

Find the extreme values of the function.  $f(x,y) = x^3 + y^3 - 3x - 12y + 2$ 

## Question: 6

Check the continuity of the following function at the point 1 and -1

$$f(x) = |x + 1| + |x - 1|$$

## **UNIT: IV**

## Question: 7

State and prove Rolle's Theorem.

## **Question: 8**

(a) If a be any finite positive number quantity, evaluate

$$\int_0^\infty \frac{e^{-x}sinmx}{x} dx$$
 and hence deduce the value of  $\int_0^\infty \frac{sinmx}{x} dx$ 

# M.Sc. First Semester STATISTICS SECOND PAPER Probability Theory Assignment

Attempt any four questions

## **UNIT-I**

Q.1) Define probability and conditional probability. State and Prove Multiplication law of probability.

Q.2) State and prove Bayes theorem and 
$$P\left(\bigcup_{i=1}^{n} A_{i}\right) \leq \sum_{i=1}^{n} P\left(A_{i}\right)$$

#### **UNIT-II**

- Q.3) What do you understand by random variables, probability mass function, probability density function, joint distribution and conditional distributions.
- Q.4) A random variable X has the following probability distribution:

$$x$$
: 0 1 2 3 4 5 6 7  $p(x)$ : 0 k 2k 2k 3k  $k^2$   $2k^2$   $7k^2+k$ 

(i) Find k, (ii) Evaluate P(X < 6),  $P(X \ge 6)$  and P(0 < X < 5), (iii) if  $P(X \le c) > \frac{1}{2}$ , find the minimum value of c and (iv) Determine the distribution function of X.

## **UNIT-III**

Q.5) What is mathematical expectation and state and proof addition theorem of expectation. If X is a random variable and 'a' is constant, then

(i) 
$$E[a\Psi(X)] = a E[\Psi(X)]$$

(ii) 
$$E[\Psi(X)+a] = E[\Psi(X)] + a$$

where  $\Psi(X)$ , a function of X, is a r.v. and all the expectations exist.

Q.6) Define moment generating function, cumulative generating function and characteristic function. State and proof Chebyshev Inequality.

## **UNIT-IV**

- Q.7) Define convergence in probability and Weak law of large numbers.
- Q.8) State and prove Central limit theorem for a sequence of independent and Borel-Cantelli Lemma.

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# M.Sc. (Statistics)

# Paper - II

# **Statistical Inference - II**

# **Assignment October 2025**

# Attempt any four questions.

## Unit – I

- Q1 Explain Pitman estimator for location.
- Q2 State and prove Hazor Bazar's theorem.

## **Unit-II**

- Q3 State and prove Lehman Schaeffer's theorem.
- Q4 Explain minimal sufficient statistics with example.

## **Unit-III**

- Q5 State and prove generalised Neyman's Lemma.
- Q6 Explain the concept of UMPU tests for the exponential family of distributions.

- Q 7 Write detail notes on Generalised Baye's Rule and Randomization optimal decision rules.
- Q8 Explain a two- person zero sum game. When it becomes a decision problem.

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M.Sc. (Statistics)

# Paper - V

# **Numerical Analysis**

# **Assignment October 2025**

# Attempt any four questions.

### Unit – I

- Q1 Derive the Newton's divided difference formula for unequal interval. How will you deduce Newton-Gregory formula from it?
- Q2 Derive the Newton Gregory formula for Backward Interpolation.

## Unit - II

Q3 Compute the value of following integral by Trapezoidal rule:

$$\int_{0.2}^{1.4} (\sin x - \log_e x + e^x) \, dx$$

Q4 Using Runge – Kutta method, solve the equation  $\frac{dy}{dx} = x + y$ , with initial condition y(0) = 1 from x = 0.1 to x = 0.4 when h = 0.1.

## Unit - III

- Q5 Derive Eular Maclaurin's summation formula.
- Q6 Use the method of inverse interpolation to find the root of the equation  $x^3$ -6x-11 = 0 that lies between 3 and 4.

- Q7 Find the real root of the equation  $x^3$ -3x-5 = 0 correct to four places of decimals by Newton Raphson method.
- Q8 Solve the system of linear equation 2x+3y+z=9, x+2y+3z=6, 3x+y+2z=8 by the factorization method.

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M.Sc. (Statistics)

# Paper -III

# Sample Surveys - I

# **Assignment October 2025**

# Attempt any four questions.

#### Unit - I

- Q1 Explain in detail the planning and execution of a large-scale survey.
- Q2 Give comparison of complete enumeration and sample surveys for collecting information of population.

## Unit - II

- Q3 Define Simple Random Sampling. Derive an unbiased estimator for population mean, variance in case of Simple Random Sampling without replacement
- Q4 Explain the purpose of stratification in sample survey. Estimate population mean and its variance for proportional and Neyman allocation.

## Unit - III

- Q5 Show that the systematic sampling is more precise than the simple random sampling, if the variance within the systematic sampling is larger than the population variance as a whole.
- Q6 What are the chief advantages and disadvantages of cluster sampling? Under what circumstances, cluster sampling is adopted.

- Q7 What is two- stage sampling. How will you estimate the variance of a two- stage estimator?
- Q8 Define ratio method of estimation. Find the variance of the estimator to the first degree of approximation.

## S.S. JAIN SUBODH P.G. COLLEGE

## (AUTONOMOUS)

## **ASSIGNMENT**

#### M.Sc Semester – III

## ATTEMPT ANY FOUR QUESTIONS

## UNIT 1

- Q1. State and prove Gauss-Markoff theorem for correlated variables.
- Q2. Give three independent stochastic variates  $y_1$ ,  $y_2$  and  $y_3$  having a common variance  $\sigma^2$  such that  $E(y_1) = \theta_1 + \theta_2$ ,  $E(y_2) = \theta_1 + \theta_3$  and  $E(y_3) = \theta_1 + \theta_2$ . Show that  $l_1 \theta_1 + l_2 \theta_2 + l_3 \theta_3$  is estimable iff  $l_1 = l_2 + l_3$ . Find an unbiased estimate of  $\sigma^2$ .

#### UNIT 2

- Q3. Prove that a connected design is balanced if all the v-1 non zero characteristic roots of c-matrix.
- Q4. Explain the general structure and analysis of block designs.

#### UN IT 3

- Q5. What do you mean by two way elimination of heterogeneity? Give the analysis of Youden square designs.
- Q6. How do you classify PBIBD designs? Give the analysis of group divisible design.

### UNIT 4

- Q7. Construct SBIBD with parameters v=b=21, r=k=5 and  $\lambda$ =1.
- Q8. For a balanced binary design with equal no. of replications. V≤b.

# S.S. Jain Subodh P.G. College, Jaipur (Autonomous)

M.Sc. (Statistics)

Semester - III

Paper – IV Econometrics

Assignment

Attempt any four questions.

### Unit - I

- Q1How do econometricians proceed in their analysis of an economic problem? Discuss the classical or traditional methodology in detail.
- Q2 What is the method of OLS of regression analysis? Discuss the assumptions underlying this method of least squares and their consequences.

## Unit - II

- Q3 Explain the nature of the problem of autocorrelation. How will you detect it? Discuss the method of generalized least squares (GLS).
- Q4 Explain graphically the nature of multicollinearity and its consequences. What are remedial measures if multicollinearity is serious?

## **Unit - III**

- Q5 Differentiate between under identification, exact identification and over identification and give one example of each. What are the rules for identification?
- Q6 What is the difference between single equation model and simultaneous equation model? Explain the problem of identification in simultaneous equation model.

- Q7 Write Short notes on Heteroscedastic disturbances and Ridge regression.
- Q8 Explain k- class estimators.